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Exercise 10

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Problem 1. Let $n \in \mathbb{N}$. If there exists a primitive element modulo n , then there exist $\varphi(\varphi(n))$ many.

Problem 2. (*properties of the discrete logarithm*) We examine the properties of the discrete logarithm.

- a) Compute the discrete logarithm of 18 and 1 in the group \mathbb{Z}_{79}^* with generator 3 (by trial and error if necessary).
- b) How many tryings would be necessary to determine the discrete logarithm in the worst case?

Problem 3. (*prove Proposition 7.5*) Prove Proposition 7.5 from the lecture, which gives a possibility to generate a primitive element modulo n :

Let $p > 3$ be prime, $p - 1 = \prod_{i=1}^k p_i^{t_i}$ the prime factorization of $p - 1$. Then,

$$a \in \mathbb{Z}_p^* \text{ is a primitive element modulo } p \Leftrightarrow a^{\frac{p-1}{p_i}} \not\equiv 1 \pmod{p} \text{ for all } i \in \{1, \dots, k\}.$$