

## Homework 12 in Cryptography I

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### Exercise 34.

Alice and Bob use the Diffie-Hellman key exchange to agree upon a shared key. As system parameters they use the prime number  $p = 101$  and the primitive element  $a = 2$  modulo  $p$ . Alice chooses as her secret  $x = 37$  and Bob chooses  $y = 33$ . Use the Square and Multiply algorithm to compute large integer powers.

- How does the protocol work? Which values must Alice and Bob exchange?
- Compute the shared key.

### Exercise 35.

How can the man-in-the-middle (MITM) attack against the DH key-exchange protocol be easily avoided?

### Exercise 36.

Alice and Bob are using the Shamir's no-key protocol to exchange a message. They agree to use the prime  $p = 31337$  for their communication. Alice chooses her random number  $r_A = 9999$  while Bob chooses  $r_B = 1011$ . Alice's message is  $m = 3567$ .

Carry out the protocol by calculating the inverses  $a^{-1} \pmod{p-1}$  and  $b^{-1} \pmod{p-1}$ . Then, compute all messages with the given values.